



A COMBINED LINEAR OPTIMISATION METHODOLOGY FOR WATER RESOURCES ALLOCATION IN AN ALFEIOS RIVER SUBBASIN (GREECE) UNDER UNCERTAIN AND VAGUE SYSTEM CONDITIONS

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OVERVIEW

- Introduction in uncertainties in water resources management

- Brief description of applied methodology (Huang et al., 1992; Li et al., 2010)



- Characteristics of the studied Alfeios River Subbasin

- Formulation of the optimisation problem



- Uncertain variable identification



- Results & Conclusions

INTRODUCTION

Uncertainties in water resources management in impact factors & system components :

- ❖ Available water resources
- ❖ Water Demand / supplies
- ❖ Related cost / benefit coefficients
- ❖ Sustainability requirements
- ❖ Policy regulations



In optimization problem:



- (A)** Decision variables
- (B)** Objective function coefficients
- (C)** Constraints coefficients

Types of uncertainty variables:

- (A)** Probability distribution
- (B)** Possibility distribution
- (C)** Interval (Upper & Lower Value)

DESCRIPTION OF METHODOLOGY



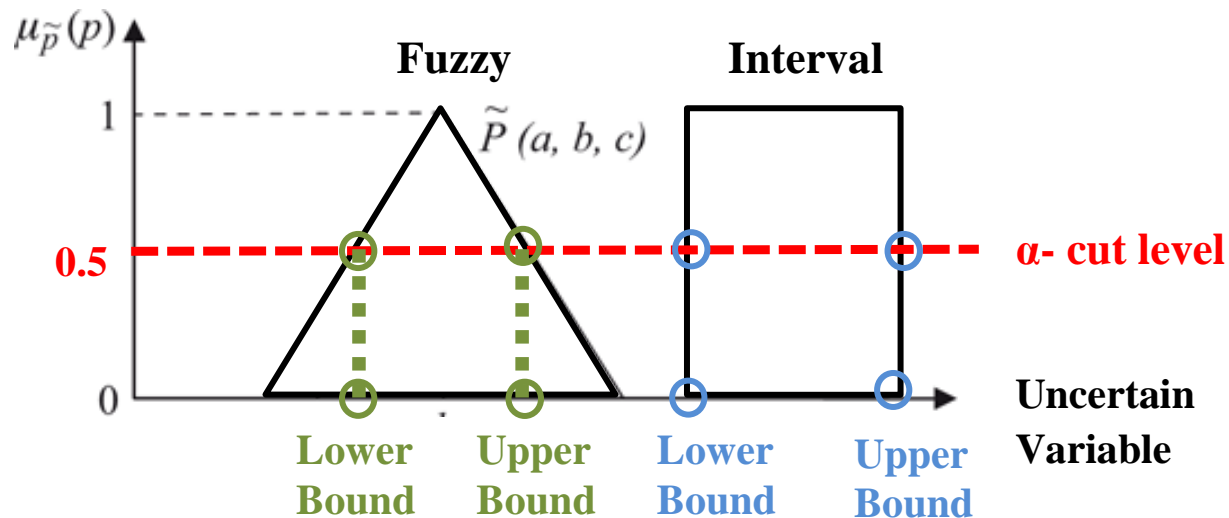
+ Fuzzy-boundary interval - stochastic programming (Li et al., 2010):

- Linear optimization problem
- Uncertain variables: (a) favourable (X_{ij}^+) & (b) unfavourable (X_{ij}^-)
- **Aim**: Identification of optimal water allocation target with minimised risk of economic penalty from water shortage (water demand) & opportunity loss from spill water volumes
- Two solution methods:
 1. “*Risk-Prone*” or “*Optimistic*” (best -case model)
 2. “*Risk-adverse*” or “*Pessimistic*” (worst -case model)

**Different solution methods imply
different risk attitudes of decision makers
considering system uncertainties**

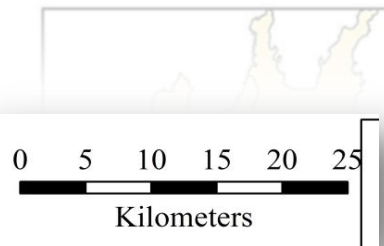
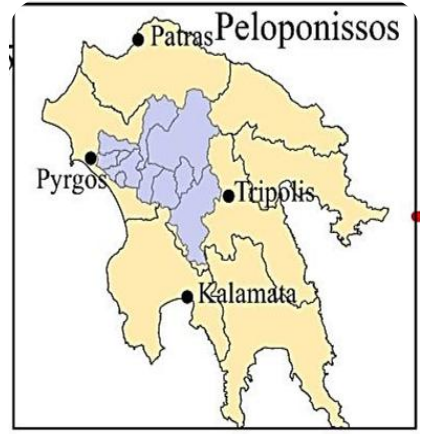
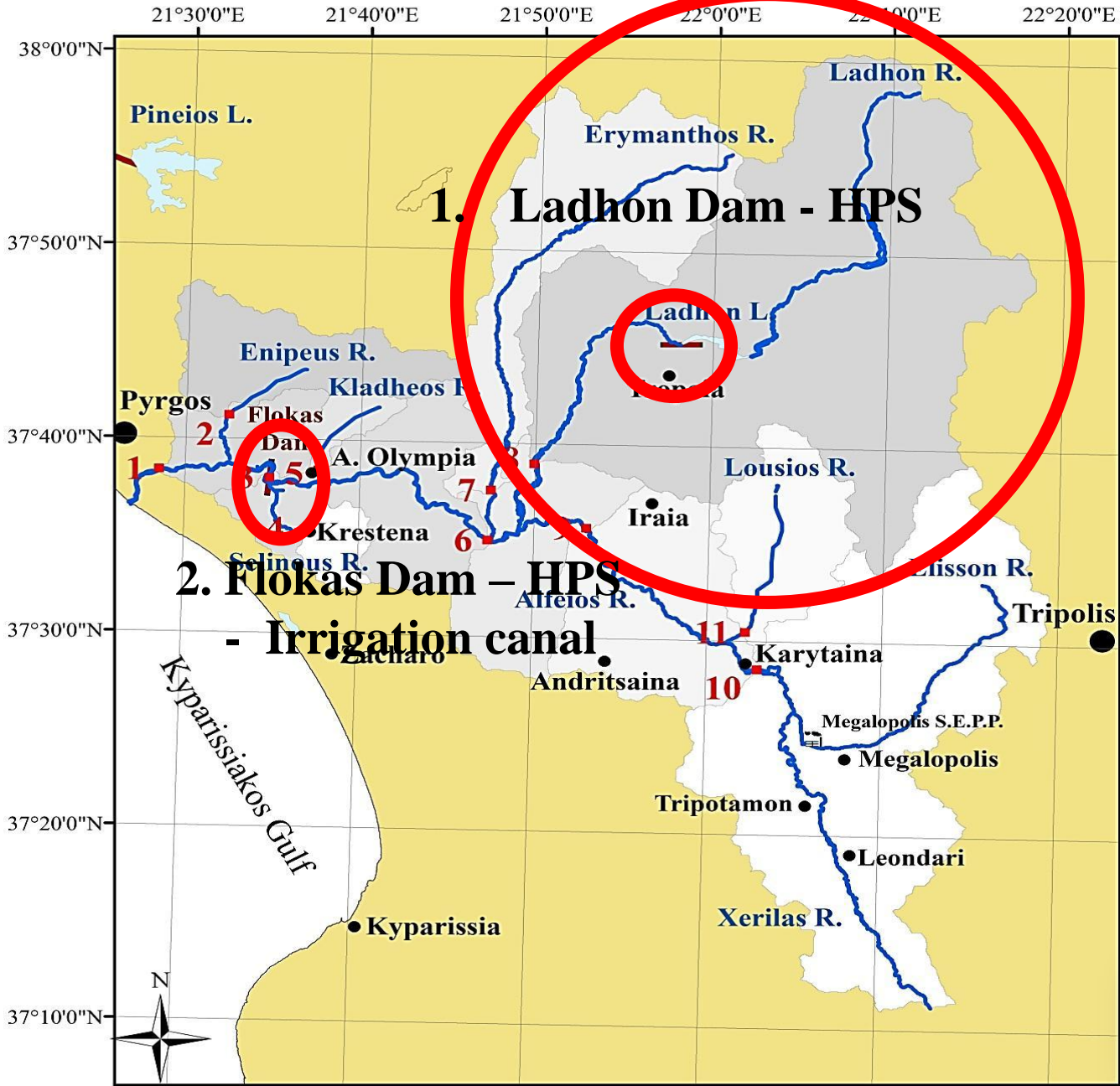
DESCRIPTION OF METHODOLOGY

- Discretization of membership grade into α -cut levels (0, 1)
- Solving for each solution type and α -cut level:
 - 2^n deterministic submodels corresponding to all combinations of lower & upper bound value for n fuzzy / interval variables



- For each solution type: $f_{\text{opt}}^{\alpha} = \{f_{\text{min}}^{\alpha}, f_{\text{max}}^{\alpha}\}$,
 where $f_{\text{min}}^{\alpha} = \min\{f_1, f_2, \dots, f_{2^n}\}$
 $f_{\text{max}}^{\alpha} = \max\{f_1, f_2, \dots, f_{2^n}\}$

EXAMINED ALFEIOS RIVER SUBBASIN



LADHON RESERVOIR & HYDROPOWER STATION

Ladhon Reservoir - Dam:

- Gross - usable storage: 57.6×10^6 - 46.2×10^6 m³
- Main purposes: Irrigation & Hydropower production
- Monthly operational curve (target reservoir level)



Ladhon Hydropower Station:

- ~8 km downstream from Ladhon Dam
- Purpose: Satisfy peak energy demand
- Total max capacity: 70 MW
- Primary & Total Mean Annual Energy: 173 & 340 GWh



FLOKAS DAM – IRRIGATION

Flokas Dam:

- Diversion dam for irrigation purposes
- 16 km from Kyparissiakos Gulf coastline
- 97% of Alfeios catchment
- Small Hydroelectric Power Station :

Max power capacity : 6.6 MW

Flokas Irrigation canal:

- Present irrigated area : 50-60% Total irrigable area (12,250 ha)
- Irrigation period : Mid April to Mid October
- Crop pattern : Cotton, corn, alfalfa, watermelons, citrus
- Surface and drip irrigation



OPTIMISATION PROBLEM

(A) Objective function:

Maximise Total Benefit :

$$\begin{aligned} & \text{Benefit(HP Ladhon)} - \text{Penalty(Spill Ladhon)} + \\ & \text{Benefit(Irrigation+Extra)} - \text{Penalty(Irrigation Shortage)} + \\ & \text{Benefit(HP Flokas)} - \text{Penalty(Spill Flokas)} \end{aligned}$$

(B) Constraints: 1. Ladhon:



- Water Volume Mass Balance
- Min & Max pumping capacity
- Min & Max reservoir storage capacity
- Evaporation: linear $F(\text{average reservoir storage}(t))$

2. Flokas: (Degree of Ladhon Contribution to Flokas)



- Water Volume Mass Balance
- Min & Max pumping capacity
- Fish ladder flows & Min environmental flows

UNCERTAIN VARIABLES

<i>VariableName</i>	<i>Uncertainty Type</i>	<i>Variable Effect</i>
Unit Benefit HP Ladhon (€/MWh)	Fuzzy: LB (40, 50, 55), UB (60, 65, 75)	Favourable
Unit Benefit HP Flokas (€/MWh)	Interval: (80, 87.75)	-
Unit Benefit Irrigation Flokas (€/m ³)	Interval: LB (0.19, 0.2), UB (0.24, 0.26)	Favourable
Unit Penalty HP Ladhon (€/MWh)	Fuzzy: LB (90, 115), LB (0.19, 0.2)	Unfavourable
Unit Penalty HP Flokas (€/MWh)	Interval: (120, 130)	-
Unit Penalty Irrigation Flokas (€/m ³)	Fuzzy: UB (0.29, 0.31), LB (0.36, 0.39)	Unfavourable
Ladhon Contribution To Flokas (%)	Interval: (0.65, 0.71)	-

For Hydropower Production Unit Benefit/ Penalty:


- operators experience Flokas: Price for small HPS
- Max observed energy sale price of Greek Energy Market

For Irrigation Unit Benefit/ Penalty (Flokas):

- Net agricultural income per crop + Irrigation water cost
- Net agricultural income per crop + Groundwater pumping costs

RESULTS

□ Optimisation using LINGO – M. Excel

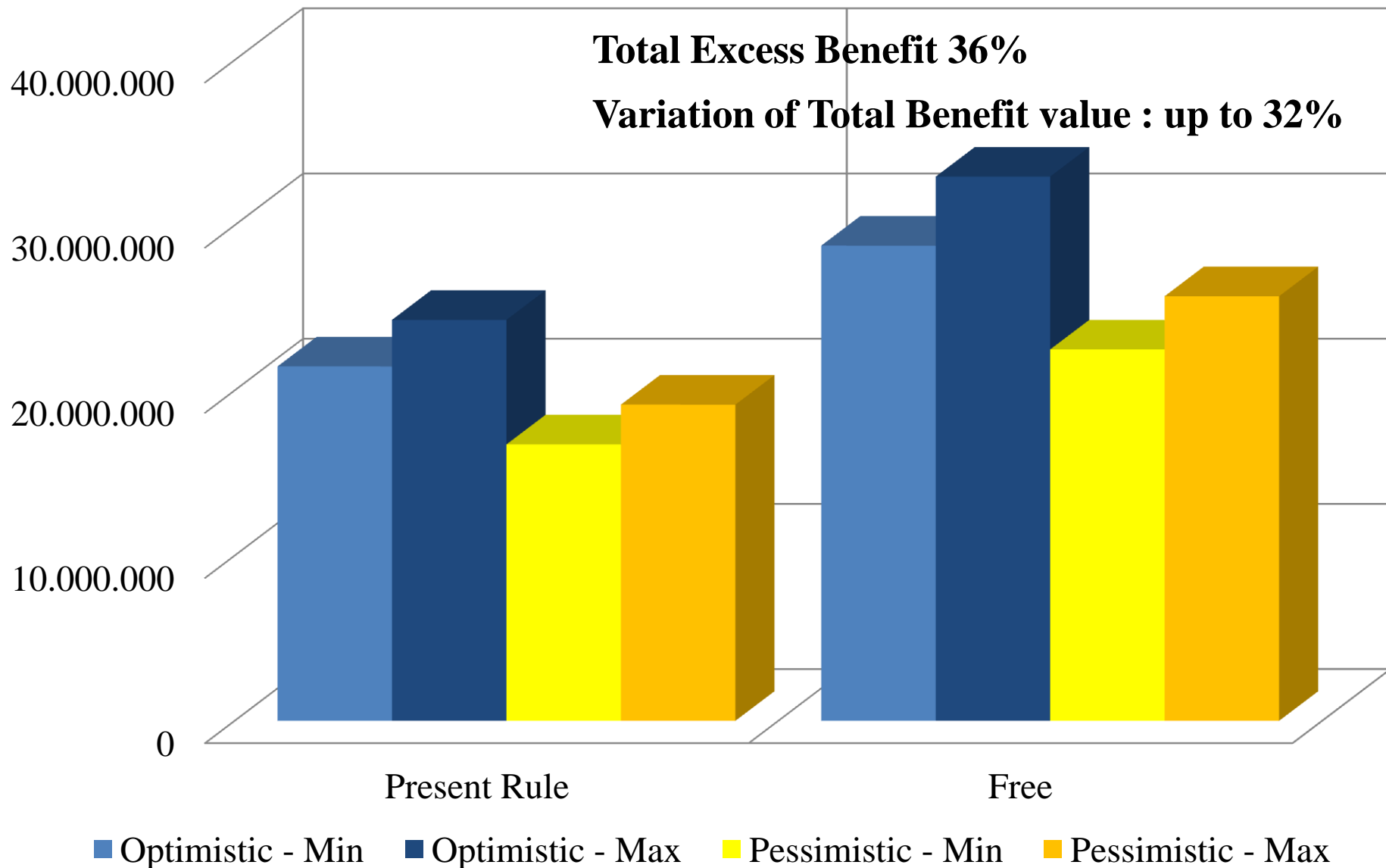
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- ❖ Available data: monthly inflows in Ladhon reservoir
(2002-2012)
 - ❖ Time step / period: Monthly / one year
 - ❖ Selection of **a.** wet year (2003)
b. dry year (2007)
 - ❖ Examined α -cut levels: 0 - 0.5 - 1
 - ❖ Total number of deterministic submodels: 576

□ Two alternative scenarios:

- 1. Present Water allocation:** Min monthly reservoir water level (Ladhon)
- 2 . Free:** No operation rule (Ladhon reservoir)

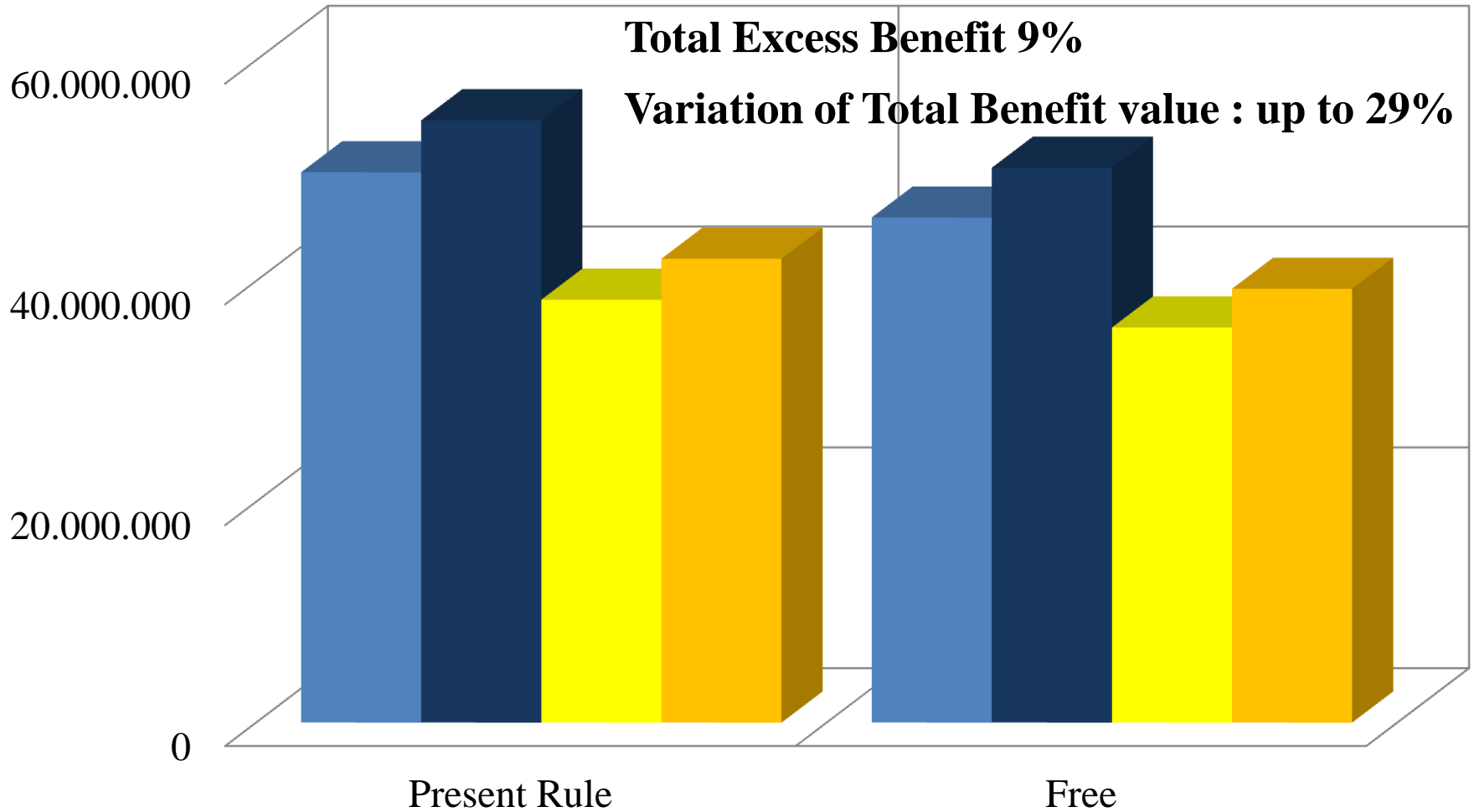
RESULTS

2007 - Total Benefit (€) for α -cut level 1



RESULTS

2003 - Total Benefit (€) for α -cut level 1



■ Optimistic - Min ■ Optimistic - Max ■ Pessimistic - Min ■ Pessimistic - Max



CONCLUSIONS

- Flexible & efficient incorporation of uncertainties (intervals and fuzzy) in linear optimisation process through α -cut levels, providing a clear & comprehensive interpretation of uncertain variable values at each stage.
- Assessment & comparison of total benefit range of various water allocation pattern for a risk-prone and risk-adverse attitudes of decision makers



OUTLOOK

- Further analysis of uncertain variables: (social benefits and non consuming water uses i.e. tourism and recreation)
- Further investigation of appropriate adjustments incorporating stochastic water inflows into methodology



When you bend down and look at the waters of the Alfeios river near Olympia, their clarity is such that your face and soul are mirrored in them... The nature becomes here spirit. The clarity of waters becomes clarity of thought ...

Panayiotis Kanellopoulos (1902-1986)

Professor of Sociology, Prime Minister of Greece

Thank you for your attention!



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